

Concept of Geometric Programming for Designing an Optimal Routing Method in Wireless Network

Neha Kumari¹, Abhishek Kumar², Arun Prasad Burnwal³

¹Department of Mathematics, Jharkhand Rai University, Ranchi, India

²Department of ECE, BIT Mesra, Ranchi, Jharkhand, India

³Department of Mathematics, GGSESTC, Bokaro, Jharkhand, India

ABSTRACT

In current scenarios, the applications of wireless network increases rapidly due to dynamic feature. Each node of this network associated with an infrastructure that helps to connect one node to another node with wirelessly within a specific range. But nodes of this network consist of limited capacity of batteries which is insufficient during any operation. So, in this paper, a routing technique is design for wireless network using geometric programming that used some strategies of game theory that help to derive an optimal route between source and destination nodes.

Keywords : Wireless Network, Geometric Programming, Game Theory, Fuzzy Logic, Routing.

I. INTRODUCTION

In last few decades, the applications of wireless network increases rapidly due to dynamic nature. It has several variation in the term of wireless ad-hoc network, wireless sensor network, vehicular ad-hoc network, hybrid ad-hoc network [1-4]. It helps in several areas such as disaster management, entertainment, business, marketing, education system, e-commerce, etc. [5-6]. The most important feature of this network is the presence of dynamic topology which will lead to the movement of the nodes. Each node of the network is consists of limited capacity of battery which is insufficient during any mission or operation, because frequently changes the place of node, energy capacity is exhaust and route or transaction is fails. In this paper, an optimal routing technique is proposed with the help of some artificial intelligence techniques. Artificial

intelligence technique is used to make a computer, or computer based program as intelligent like human. It helps to take decision in the situation where information is full of uncertainty and imprecise [7-8]. In this paper, three basic elements of artificial intelligence technique are used such as game theory, geometric programming, and fuzzy logic. Game theory is a part of mathematical modelling which is used to model the competitive situation in form of mathematic where set of players are take the decision based on conflicting strategies [9-10]. Geometric programming is a non-linear programming which is used to combine objective functions and their related constraints in the form of posynomial instead of polynomial [11]. Fuzzy logic is a part of soft computing which produce soft answer instead of had answer, where soft answer indicates approximation based result and hard answer indicates rigid solution [12-14]. The issues raised in the wireless network are

full of uncertainty and imprecise related information where characteristic of hard computing is fails and characteristic of soft computing is pass. [15-18]. The combination of these three artificial intelligence techniques produce a solution where we can easily find the optimal routing technique in the wireless network.

II. RELATED WORKS

Energy efficient routing is the main challenges of the ad-hoc network. There have been lot of works are done on energy efficient routing such as Wei et al. [19] proposed a new optimized priority based energy efficient routing algorithm PDSR. The main aims of this algorithm to add priority to the existing routing algorithm according to the residual energy proportion of the nodes. Lower residual energy means lower priority and the nodes with lower priority are less likely to forward packets to other nodes. It can also improve the performance of routing discovery, routing maintenance and route cache. But it has a limitation that hop count and distance are not considered for improvement and route maintenance. Su et al. [20] proposed the fuzzy logic modified AODV routing (FMAR) protocol for multicast routing in mobile ad-hoc networks. The main aim of this protocol is dynamically evaluate the active routes based on fuzzy logic weighted multi-criteria. It also helps to managing the limited bandwidths of wireless links. But it has some drawback that the proposed protocol does not considered all possible routes as evaluation of route lifetime by fuzzy logic multi-criteria, so it cannot be determine which routes are highly useful. Therefore, routes cannot repair and maintain partially or completely before they crashed. Matthew J. Miller and Nitin H. Vaidya [21] proposed a link layer protocol to provide k levels of power save and a routing protocol to use this link layer effectively. In this protocol the authors first to generalize the concept for ad-hoc networks by proposing the use of k levels of power save, each of which presents a

different energy-latency tradeoff. Thus, previous work [22-25] only considered the case where $k = 1$ or $k = 2$. Guo et al. [26] proposed a multi-objective approach for proactive routing in a MANET. In this approach, the authors consider three routing objectives: minimizing average end-to-end delay, maximizing network energy lifetime, and maximizing packet delivery ratio. For the proposed multi-objective approach, the authors developed two efficient prediction methods first predicting queuing delay and energy consumption using double exponential smoothing, and second predicting residual link lifetime using a heuristic of the distributions of the link lifetimes in MANET. Kalantari et al. [27] proposed a soft computing method (RWSN) for energy efficient routing in wireless sensor network. The main aim of this method to determines reward of each route using reward function based on two parameters energy and distance. This function determines which actions have been good and which have been loaded. It gives a number to each pair (state/action). The action is good indicating that energy is high and distance is short. The action is loaded indicating that energy is low and distance is long. The reward function in this proposed system is obtained through fuzzy logic system. But it has some drawback that the proposed method does not considered hop count and data packet as parameters of energy efficient routing. R.Vadivel and V. Murali Bhaskaran [28] proposed a protocol EESRRP for MANET. The main aim of this protocol is that residual energy metric is estimated for providing energy efficiency and improved reliability. It also helps to provide security against malicious attacks using an effective intercept detection and correction (IDC) algorithm. Das et al. [29] proposed a soft computing method (ERPC) for energy efficient routing in wireless sensor network. The main aims of this method to demonstrate a strategy of power consumption system in wireless sensor network by using the concept of complete bipartite graph. The basic parameters of this strategy are power and distance. Finally, it assigns priority to

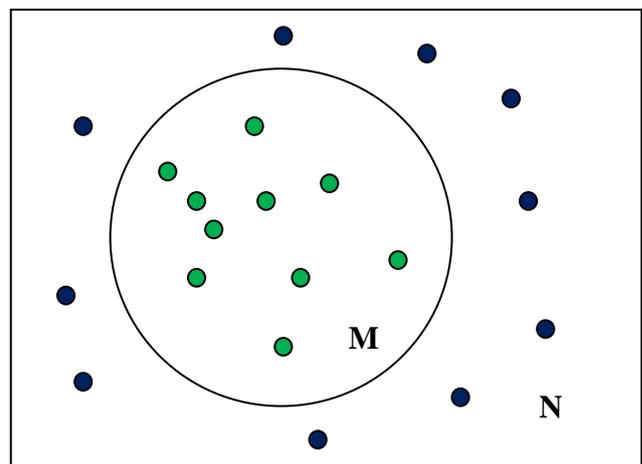
each route and determines the best and worst routing in wireless sensor network. But it has some limitation that the proposed method does not considered hop count and data packet as parameters of energy efficient routing. Because energy efficient routing not considering only energy and distance, it also cover hop count and transmitter packet. Das et al. [30] proposed a method (IECR) for energy efficient routing in wireless sensor network. The main aims of this method to generate some values for each and every route based on fuzzy inference engine. This values determine the different nature of the routes. Therefore, this value helps to determine which route is best and which route is worst for routing in term of energy efficiency. But it has some limitation that the proposed method does not considered hop count and data packet as parameters of fuzzy inference engine. Because energy efficient routing cannot determines by using two parameters such as energy and distance.

However, none of the technique derived an optimal routing by combing strategies of the nodes in non-linear formulation. So, proposed method pave the gap of the earlier method. Several preliminaries are used in the proposed method such as game theory, geometric programming, and fuzzy logic. Game theory is used to model the conflicting strategy of the network with the help of player, strategy, and utility function where nodes are play the role of players, network conflicting situations are play the role of strategies, and used techniques for selecting optimal route are play the role of utility functions. Geometric programming is a non-linear programming which works in posynomial environment instead of polynomial environment. It helps to estimates non-linear parameters of the network efficiently.

III. PROPOSED ROUTING METHOD

The proposed network model consider as a graph $G(N,E)$ where N is a set of nodes and E is a set of edges. Each node of this network associated within

range shown in Fig. 1. In this figure M is indicates one radio range that consist of some nodes and N indicates out of radio range that also consist of some nodes. Moreover, the nodes in M can communicate one to another and able to send/receive data packet, but the nodes in N cannot communicate one to another and not able to send/receive data packet.



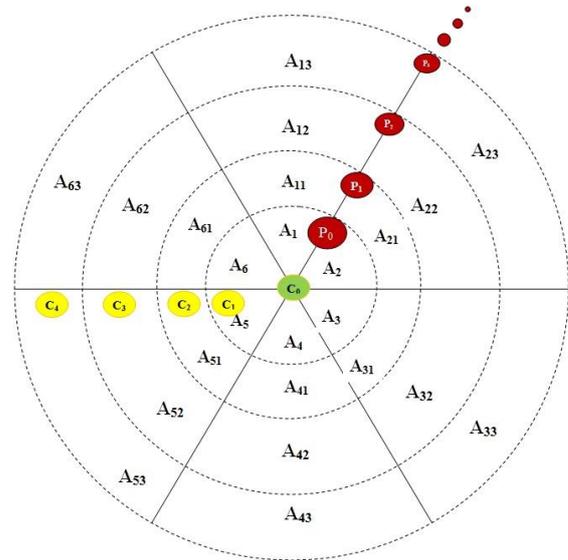
Caption:
● Inside ●

Fig. 1: Zone of the network model.

The framework of the proposed method divided by clustered mechanism. Each cluster is divided into two basic zones Zone 1 (i.e. M) and Zone 2 (i.e. N) because there is no any node that control and manage to all nodes of the proposed framework. The distribution of different nodes within network is bounded different clustered areas C_1, C_2, C_3, C_4 shown in Fig. 2. Each and every clustered distributed in Zone 1 of proposed system model are enclosed by cluster such as areas $A_1, A_2, A_3, A_4, A_5, A_6$ enclosed by cluster C_1 , the next areas $A_{11}, A_{21}, A_{31}, A_{41}, A_{51}, A_{61}$ enclosed by cluster C_2 , the next areas $A_{12}, A_{22}, A_{32}, A_{42}, A_{52}, A_{62}$ enclosed by cluster C_3 , the next areas $A_{13}, A_{23}, A_{33}, A_{43}, A_{53}, A_{63}$ enclosed by cluster C_4 and so on, where 'C₀' encloses no wireless node, it contains the center node which is fixed. The wireless network is not connected with any wired and it is not fixed, position of the node is changes based on the requirement of the users. So, here crisp logic is not

employed, instead of crisp logic the parameters of the network are used fuzzy logic, because fuzzy logic deals with partial true and partial false which range between 0 and 1. Hence, membership functions of some network parameters such as energy, distance, mobility, and overhead are shown in Table 1 to Table 4. These network parameters are known as input parameter. Each membership function of input parameter is divided into nine linguistic variables as Very Low, Quite Low, Low, Quite Medium, Medium, Less High, Quite High, High, Very High. In this proposal, output variable is consider as network lifetime that depends on two types natures as Nature 1 and Nature 2. The input parameters energy and distance are considered in Nature 1 and another two input parameters mobility and overhead are considered in Nature 2. The output parameter network lifetime is also divided into nine linguistic variables such as Poor, Very Bad, Bad, Less Medium, Medium, Good, Very Good, Outstanding, and Excellent. The details of both natures predicted as fuzzy rules that shown in Table 5 and Table 6. In the proposed method, nodes of the network work as players and different conflicting situations are work as strategies. The function which is derive the optimal routing is known as utility function. Eq. 1 indicates the set of players, Eq. 2. Indicates set of strategies, Eq. 3 indicates set of utility functions. The combination of game theory strategy and non-linear formulation of geometric programming helps to

implement the proposed method. Table 7 shows different considered strategies of the players. The network having one or more objective depends on the situation, so, the proposed equations shows in Eqs. 4 and 5. The actual optimal route is derives by the help of higher rank of nature 1 and nature 2 conditions that defined in Tables 5 and 6.



Caption:
● Center node ● Cluster ● Stable node

Fig 2: Clustering framework model.

Table 1: Membership function of energy.

Linguistic Values	Notation	Range
Very Low	VLE	[VLE _a , VLE _b]
Quite Low	QLE	[QLE _a , QLE _b]
Low	LE	[LE _a , LE _b]
Quite Medium	QME	[QME _a , QME _b]
Medium	ME	[ME _a , ME _b]
Less High	LHE	[LHE _a , LHE _b]
Quite High	QHE	[QHE _a , QHE _b]
High	HE	[HE _a , HE _b]
Very High	VHE	[VHE _a , VHE _b]

Table 2: Membership function of distance.

Linguistic Values	Notation	Range
Very Low	VLD	[VLD _a , VLD _b]
Quite Low	QLD	[QLD _a , QLD _b]
Low	LD	[LD _a , LD _b]
Quite Medium	QMD	[QMD _a , QMD _b]
Medium	MD	[MD _a , MD _b]
Less High	LHD	[LHD _a , LHD _b]
Quite High	QHD	[QHD _a , QHD _b]
High	HD	[HD _a , HD _b]
Very High	VHD	[VHD _a , VHD _b]

Table 3: Membership function of mobility.

Linguistic Values	Notation	Range
Very Low	VLM	[VLM _a , VLM _b]
Quite Low	QLM	[QLM _a , QLM _b]
Low	LM	[LM _a , LM _b]
Quite Medium	QMM	[QMM _a , QMM _b]
Medium	MM	[MM _a , MM _b]
Less High	LHM	[LHM _a , LHM _b]
Quite High	QHM	[QHM _a , QHM _b]
High	HM	[HM _a , HM _b]
Very High	VHM	[VHM _a , VHM _b]

Table 4: Membership function of overhead.

Linguistic Values	Notation	Range
Very Low	VLO	[VLO _a , VLO _b]
Quite Low	QLO	[QLO _a , QLO _b]
Low	LO	[LO _a , LO _b]
Quite Medium	QMO	[QMO _a , QMO _b]
Medium	MO	[MO _a , MO _b]
Less High	LHO	[LHO _a , LHO _b]
Quite High	QHO	[QHO _a , QHO _b]
High	HO	[HO _a , HO _b]
Very High	VHO	[VHO _a , VHO _b]

Table 5: Fuzzy rules for nature 1.

Rule no.	Antecedent	Consequent	Rank no.
Rule 1	If Energy is VLE and Distance is VHD	Network lifetime Poor	Rank 9
Rule 2	If Energy is QLE and Distance is HD	Network lifetime Very Bad	Rank 8
Rule 3	If Energy is LE and Distance is QHD	Network lifetime Bad	Rank 7
Rule 4	If Energy is QME and Distance is LHD	Network lifetime Less Medium	Rank 6
Rule 5	If Energy is ME and Distance is MD	Network lifetime Medium	Rank 5
Rule 6	If Energy is LHE and Distance is QMD	Network lifetime Good	Rank 4
Rule 7	If Energy is QHE and Distance is LD	Network lifetime Very Good	Rank 3
Rule 8	If Energy is HE and Distance is QLD	Network lifetime Outstanding	Rank 2
Rule 9	If Energy is VHE and Distance is VLD	Network lifetime Excellent	Rank 1

Table 6: Fuzzy rules for nature 2.

Rule no.	Antecedent	Consequent	Rank no.
Rule 1	If Mobility is VLM and Overhead is VHO	Network lifetime Poor	Rank 9
Rule 2	If Mobility is QLM and Overhead is HO	Network lifetime Very Bad	Rank 8
Rule 3	If Mobility is LM and Overhead is QHO	Network lifetime Bad	Rank 7
Rule 4	If Mobility is QMM and Overhead is LHO	Network lifetime Less Medium	Rank 6
Rule 5	If Mobility is MM and Overhead is MO	Network lifetime Medium	Rank 5
Rule 6	If Mobility is LHM and Overhead is QMO	Network lifetime Good	Rank 4
Rule 7	If Mobility is QHM and Overhead is LO	Network lifetime Very Good	Rank 3
Rule 8	If Mobility is HM and Overhead is QLO	Network lifetime Outstanding	Rank 2
Rule 9	If Mobility is VHM and Overhead is VLO	Network lifetime Excellent	Rank 1

Table 7: Strategy description of the nodes.

Strategy	Description
Wait	This strategy indicates the node still waiting for acknowledgement.
Sleep	It is energy saving mode when node is not working.
Running	It is working mode when node either send or receive the data packets.
Dead	It is energy less mode when battery capacity is fully exhaust.

$$N=\{n_1, n_2, n_3, \dots \lambda_1\} \tag{1}$$

$$S=\{s_1, s_2, s_3, \dots \lambda_2\} \tag{2}$$

$$U=\{u_1, u_2, u_3, \dots \lambda_3\} \tag{3}$$

$$\begin{aligned} \text{Optimize} \quad & f(x)=(f_1(x), f_2(x), \dots f_k(x))^T \\ \text{subject to} \quad & g_j(x) \leq b_j, \text{ where } j=1, 2, 3, \dots, n \\ & X=(x_1, x_2, x_3, \dots, x_n) \geq 0 \end{aligned} \tag{4}$$

$$\text{flow}(n_i, n_j) \geq 0, \forall n_i \leftrightarrow n_j \in E \tag{5}$$

Hence, final optimal route is considered by combining two situations: (i) when energy is very high and distance is very low, (ii) when mobility is very high and overhead is very low. Due to dynamic nature and high confliction condition second choice also considered as (iii) when energy is high and distance is quite low, (iv) when mobility is high and overhead is quite low.

The optimization level of the proposed model is non-linear.

Table 8: Simulation parameters.

Parameter	Description
LINGO software version	15.0
MS Office	2013
Chart	Bar graph
Graph	2-D
Optimization model	Non-linear

IV. PERFORMANCE EVALUATION

The performance of the proposed method is compared with linear model. The proposed model is simulated in LINGO optimization software which is licensed based optimization software. The simulation parameters are shown in Table 8. The version of LINGO software is 15.0, the graph is drawn in MS Excel 2013, and type of graph is chosen is bar chart.

The wireless network is consists of several types of nodes that may be static or dynamic. The wireless network sometime connects with some static or wired network. So, sometimes conflicting arise frequently due to concoction nature of the network elements and its topology. The performance of the wireless network is depends on several network parameters but among all the parameters, energy is the vital parameter which is sometimes known as a

residual energy. This parameter effects all other parameters including network lifetime. In this paper, energy consumption is evaluated based on fusion of game theory strategy and non-linear geometric programming formulation.

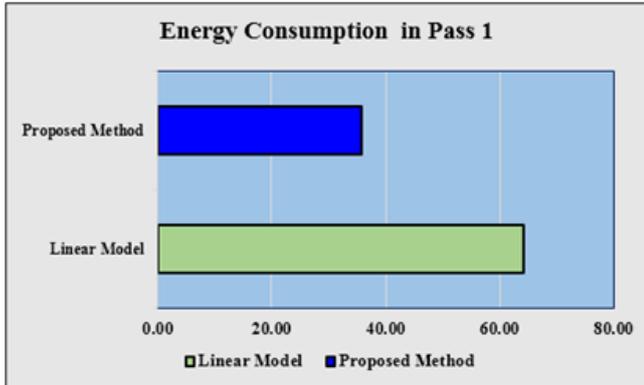


Fig 3: Energy consumption in Pass 1.

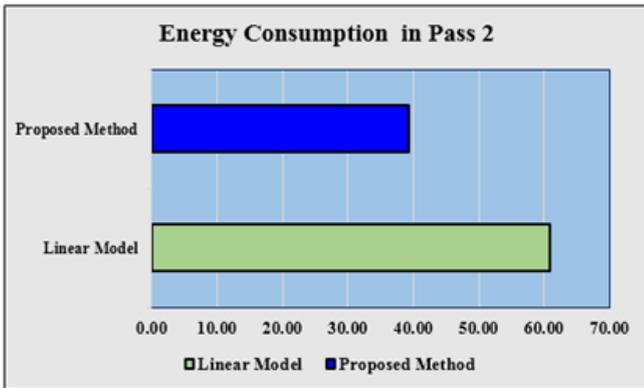


Fig 4: Energy consumption in Pass 2.

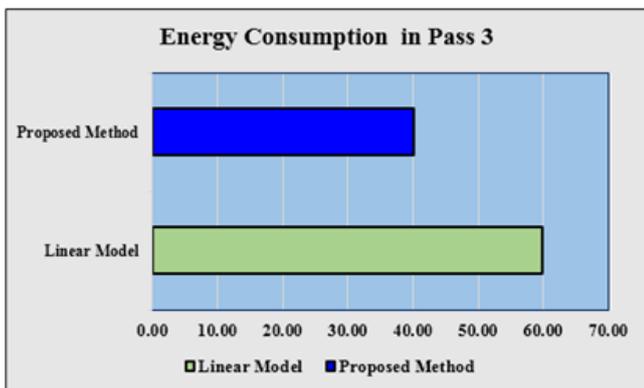


Fig 5: Energy consumption in Pass 3.

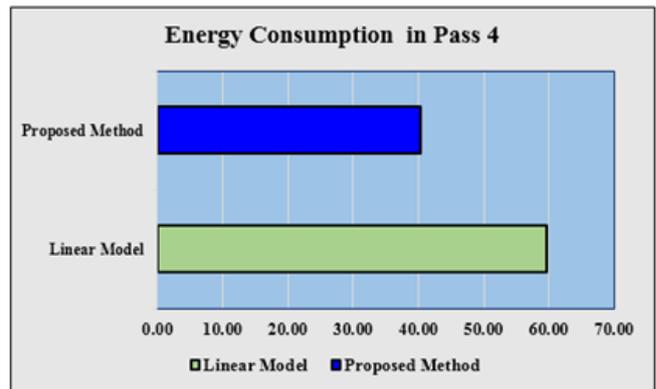


Fig 6: Energy consumption in Pass 4.

Energy consumption is the amount of energy consumed during a process. It covered energy consumed during transmit data packet as well as send data packet. The proposed model is evaluated in four iterations shown in Figs. 3 to 6 by modelling two ways such as linear method, and proposed method. We observe that energy consumption is significantly reduced in each iteration of the proposed method.

V. CONCLUSION

In this paper, an optimal routing technique is design for wireless network with the help of three methods such as game theory strategy, geometric programming and fuzzy logic. Strategy of the game theory is used to model all conflicting strategies of the network, geometric programming is used to model all non-linear parameters of the network, fuzzy logic is used to make imprecise goals of the network. The combination of these methods helps to derive an optimal routing which enhance the network lifetime by reducing less energy of the nodes.

VI. REFERENCES

- [1] S. K. Das and S. Tripathi, "Intelligent energy-aware efficient routing for MANET," Wireless Networks, 2016, pp. 1-21, DOI 10.1007/s11276-016-1388-7.
- [2] S. K. Das, A. K. Yadav and S. Tripathi, "IE2M: Design of intellectual energy efficient multicast

- routing protocol for ad-hoc network,” *Peer-to-Peer Networking and Applications*, 2016, vol. 10, no. 3, pp. 670-687, DOI 10.1007/s12083-016-0532-6.
- [3] A. K. Yadav, S. K. Das and S. Tripathi, “EFMMRP: Design of efficient fuzzy based multi-constraint multicast routing protocol for wireless ad-hoc network,” *Computer Networks*, 2017, vol. 118, pp. 15-23, <https://doi.org/10.1016/j.comnet.2017.03.001>.
- [4] Boukerche, Azzedine, et al. "Vehicular ad hoc networks: A new challenge for localization-based systems." *Computer communications* 31.12 (2008): 2838-2849.
- [5] S. K. Das, A. Kumar, B. Das, and A. Burnwal, “Ethics of reducing power consumption in wireless sensor networks using soft computing techniques,” *International Journal of Advanced Computer Research*, 2013, vol. 3, no. 1, pp. 301-304.
- [6] S. K. Das, S. Tripathi, and A. Burnwal, “Intelligent energy competency multipath routing in wanet,” in *Information Systems Design and Intelligent Applications*, Springer, 2015, pp. 535-543, DOI: 10.1007/978-81-322-2250-7_53.
- [7] S. K. Das and S. Tripathi, “Energy efficient routing formation technique for hybrid ad hoc network using fusion of artificial intelligence techniques,” *International Journal of Communication Systems*, 2017, pp. 1-16, DOI: 10.1002/dac.3340.
- [8] A. Burnwal, A. Kumar, and S. K. Das, “Survey on application of artificial intelligence techniques,” *International Journal of Engineering Research & Management*, 2014, vol. 1, no. 5, pp. 215-219.
- [9] S. K. Das and S. Tripathi, “Adaptive and intelligent energy efficient routing for transparent heterogeneous ad-hoc network by fusion of game theory and linear programming,” *Applied Intelligence*, 2017, pp. 1-21, <https://doi.org/10.1007/s10489-017-1061-6>.
- [10] A. Burnwal, A. Kumar, and S. K. Das, “Assessment of Mathematical Modeling in Different Areas,” *International Journal of Advanced Technology & Engineering Research*, 2013, vol. 3, no. 3, pp. 23-26.
- [11] S. K. Das and S. Tripathi, “Energy efficient routing formation algorithm for hybrid ad-hoc network: A geometric programming approach,” *Peer-to-Peer Networking and Applications*, 2018, pp. 1-27, <https://doi.org/10.1007/s12083-018-0643-3>.
- [12] S. K. Das, S. Tripathi, and A. Burnwal, “Fuzzy based energy efficient multicast routing for ad-hoc network,” in *Computer, Communication, Control and Information Technology (C3IT), 2015 Third International Conference on*, IEEE, 2015, pp. 1-5, DOI: 10.1109/C3IT.2015.7060126.
- [13] S. K. Das, S. Tripathi, and A. Burnwal, “Design of fuzzy based intelligent energy efficient routing protocol for WANET,” in *Computer, Communication, Control and Information Technology (C3IT), 2015 Third International Conference on*, IEEE, 2015, pp. 1-4, DOI: 10.1109/C3IT.2015.7060201.
- [14] A. Burnwal, A. Kumar, and S. K. Das, “Assessment of fuzzy set theory in different paradigm,” *International Journal of Advanced Technology & Engineering Research*, 2013, vol. 3, no. 3, pp. 16-22.
- [15] S. K. Das and S. Tripathi, “Energy efficient routing protocol for manet based on vague set measurement technique,” *Procedia Computer Science*, 2015, vol. 58, pp. 348-355, doi:10.1016/j.procs.2015.08.030.
- [16] S. K. Das and S. Tripathi, “Energy Efficient Routing Protocol for MANET Using Vague Set,” in *Proceedings of Fifth International Conference on Soft Computing for Problem Solving*, Springer, 2016, pp. 235-245, DOI: 10.1007/978-981-10-0448-3_19.
- [17] S. K. Das, A. Kumar, B. Das, and A. Burnwal, “On soft computing techniques in various areas,”

- Computer Science & Information Technology (CS & IT), 2013, vol. 3, pp. 59-68, DOI : 10.5121/csit.2013.3206.
- [18] S. K. Das, S. Tripathi, and A. Burnwal, "Some relevance fields of soft computing methodology," *International Journal of Research in Computer Applications and Robotics*, 2014, vol. 2, pp. 1-6.
- [19] Xiaohai Wei, Guoliang Chen, Yingyu Wan and Fred Mtenzi, "Optimized priority based energy efficient routing algorithm for mobile ad hoc networks." *Ad Hoc Networks* 2.3 (2004): 231-239.
- [20] Bey-Ling Su, Ming-Shi Wang and Yueh-Ming Huang, "Fuzzy logic weighted multi-criteria of dynamic route lifetime for reliable multicast routing in ad hoc networks." *Expert Systems with Applications* 35.1 (2008): 476-484.
- [21] Matthew J. Miller and Nitin H. Vaidya "Ad hoc routing for multilevel power save protocols." *Ad Hoc Networks* 6.2 (2008): 210-225.
- [22] R. Zheng, R. Kravets, On-demand power management for ad hoc networks, in: *IEEE Infocom 2003*, April 2003.
- [23] C. Sengul, R. Kravets, TITAN: On-demand topology management in ad hoc networks, *ACM Mobile Computing and Communications Review (MC2R)* 9 (1) (2005) 77-82.
- [24] B. Chen, K. Jamieson, H. Balakrishnan, R. Morris, Span: An energy-efficient coordination algorithm for topology maintenance in ad hoc wireless networks, in: *ACM Mobi-Com 2001*, July 2001.
- [25] Y. Xu, J. Heidemann, D. Estrin, Geography-informed energy conservation for ad hoc routing, in: *ACM MobiCom 2001*, July 2001.
- [26] Zhihao Guo , Shahdi Malakooti, Shaya Sheikh, Camelia Al-Najjar and Behnam Malakooti, "Multi-objective OLSR for proactive routing in MANET with delay, energy, and link lifetime predictions." *Applied Mathematical Modelling* 35.3 (2011): 1413-1426.
- [27] Samira Kalantari, Mohsen Amiri besheli, Zeinab Sam Daliri, Shahaboddin Shamshirband and Liang Shing Ng, "Routing in wireless sensor network based on soft computing technique." *Scientific Research and Essays* 6.21 (2011): 432-4441.
- [28] R.Vadivel and V. Murali Bhaskaran, "Energy efficient with secured reliable routing protocol (EESRRP) for mobile ad-hoc networks." *Procedia Technology* 4 (2012): 703-707.
- [29] S. K. Das, A. Kumar, B. Das, and A. Burnwal, "Ethics of E-Commerce in Information and Communications Technologies," *International Journal of Advanced Computer Research*, 2013, vol. 3, no. 1, pp. 122-124, doi=10.1.1.300.9397.
- [30] S. K. Das, B. Das, and A. Burnwal, "Intelligent energy competency routing scheme for wireless sensor networks", *International Journal of Research in Computer Applications and Robotics*, 2014, vol. 2, no. 3, pp. 79-84.