



Enhancement of Signature Schemes for Heightening Security in Blockchain

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ABSTRACT

Blockchain has become one of the most pioneering technologies, with the rise of Bitcoin, blockchain which is the core technology of Bitcoin has received increasing attention. There are multiple signature scheme based on digital signature schemes that supports making signatures on many different messages generated by many different users, the size of the signature could be shortened by compressing multiple signatures into a single signature. Based on the blockchain architecture and existing Merkle tree based signature schemes, In this paper, an analysis of how to enhance the signature schemes to secure the transactions on blockchain based on extensible post-quantum (PQ) resistant digital signature scheme best suited to blockchain and distributed ledger technologies is proposed.

I. INTRODUCTION

Recent advances in quantum computing and the threat this poses to classical cryptography has increased the interest in PQ research. More specifically, due to Shor's algorithm [1], a quantum computer could easily factor a big integer in polynomial time, thus effectively break RSA. Implementations of Shor's algorithm can also solve discrete logarithms and render today's digital signatures, such as DSA, ECDSA and EdDSA, useless[2].

The race to build quantum computers has already begun and companies like Google, Microsoft, IBM, D-Wave and Intel are at the forefront. That being said, we have yet to build a computer with the thousands of stable qubits that are required to make classical public key cryptography obsolete. However, there is significant progress in the field and some

optimistic predictions estimate that a large quantum computer capable of breaking asymmetric cryptography might be available in the next 10 to 20 years [3], [4].

The security impact of breaking public key cryptography would be tremendous, as almost everything from HTTPS, VPN and PKI in general, is basing their authentication, key exchange and digital signatures on the security of RSA or Elliptic Curve Cryptography (ECC). Blockchains would be hit equally hard resulting in broken keys that hold coins/assets, and would perhaps be one of the most affected sectors because there is economic incentive for hackers to get access to blockchain accounts anonymously.

To address the concern of compromised keys, PQ cryptography is dealing with the design and evaluation of systems that will survive the quantum

supremacy. An enhanced solution is a modified version of the hash-based XMSS [5] family of schemes. It practically makes use of a single authentication path; thus, it is a chain and not a tree and it mainly focuses on {one and limited}-time keys, which is usually the most applicable to blockchains as we want to preserve anonymity and minimise tracking.

Compared to existing schemes, the approach outperforms limited-time schemes when required to sign only once or a few times. Unlike one-time schemes (OTS), this scheme provides a fallback mechanism to easily support many-time signatures. Moreover, the underlying logic of a “blockchained” authentication path could be applied to convert any existing hash-based scheme to a {one and/or few}-time optimised one. To our knowledge, this is the first signature scheme that can utilise an existing blockchain or graph structure to reduce the signature cost to one OTS, even when we plan to sign many times. This makes existing many-time stateful signature schemes obsolete for blockchain applications. Moreover, the scheme is solely based on hash functions and that no special math theory is required for its implementation makes it a promising candidate for existing or new blockchain applications, and for low-end devices, such as in IoT applications, where hashing operations are already implemented and sometimes hardware optimized.

II. HASH FUNCTION IN BLOCKCHAINS

A cryptographic hash function is an algorithm that maps data of arbitrary size to a fixed size string. Two security requirements named one-wayness and collision-resistance are usually required for hash functions. The former ensures that the underlying hash function is not invertible, while the latter implies that it is not easy to find two inputs having the same hash value. For a hash function with n -bit length output, the complexities of breaking one-wayness and finding a collision are respectively bounded by $O(2^n)$ brute force attack and

$O(2^{n/2})$ birthday attack. Therefore, for ensuring at least 80-bit security, the output length of hash functions should be at least 160 bits. The most popular hash function used in blockchains is SHA256, which is one of the algorithms from a family of cryptographic hash functions named SHA (Secure Hash Algorithms). SHA is a U.S. Federal Information Processing Standard, and most of the algorithms in this family, including SHA0 (published in 1993), SHA1 (published in 1995), SHA2 (published in 2001) are designed by the United States National Security Agency (NSA). While SHA3 (published in 2014) is original from Keccak proposed by (Bertoni et al., 2010), and only the padding method is modified by the National Institute of Standards and Technology (NIST). To satisfy the current security requirement, SHA2 and SHA3 are recommended for using in blockchains and cryptocurrencies.

III. DIGITAL SIGNATURES

Besides the hash function, the digital signature is another inevitable cryptographic primitive in blockchains. The concept of the digital signature was put forward by Diffie and Hellman in 1976 when they opened the gate of public key cryptography (Diffie and Hellman, 1976). As a basic primitive of cryptography, digital signature is used for ensuring the source authentication (Lin et al., 2018), source non-repudiation and integrity. The standard security of the digital signature is existential unforgeability against adaptively chosen messages attacks (EUF-CMA), which guarantees that the adversary cannot forge a valid signature on a new message, even if it can access the signing oracle that could provide the signing service. ECDSA (Certicom-Research, 2000) and EdDSA (Bernstein et al., 2011) are the two digital signature schemes frequently used in blockchains. In principle, both of them are based on the hardness of the elliptic curve version of discrete logarithm problem. ECDSA works over a general elliptic curve and now is used in Bitcoin and Ethereum, while EdDSA works over a (twisted) Edwards curve and now is used in Naïve coin and

Monero. The Edwards curve is a plane model of an elliptic curve and has better efficiency and security than a general elliptic curve. Thus, it has been already selected as the next elliptic curve generation of TLS by Internet Research Professional Working Group.

IV. SPECIAL SIGNATURE PRIMITIVES FOR BLOCKCHAINS

To enhance the privacy and anonymity of transactions, some advanced signature primitives such as ring signature and multi-signature are also widely applied in blockchains

4.1 Ring signatures

Anonymity is always required in information systems (Shen et al., 2018), especially in the e-cash system. However, Bitcoin can only provide pseudonymity due to the linkability of transactions. Therefore, many new alternative cryptocurrencies have been proposed to address this problem. From a perspective of cryptography, there are many kinds of signatures for achieving anonymity, such as blind signature (Chaum, 1982), ring signature (Rivest et al., 2001), group signature (Chaum and van Heyst, 1991) and DC-nets (Chaum, 1988). However, only ring signature and its variants have been used in blockchains for anonymity. The concept of ring signature was proposed in 2001 by Rivest, Shamir and Tauman (Rivest et al., 2001). One can use a ring signature scheme to sign messages on behalf of a group including him-self/herself without revealing himself/herself, while he/she can compose this group without other group members' permission. Besides the existential unforgeability, the unconditional anonymity is another important security requirement for ring signature. This new property can be divided into two sub-properties: untraceability and unlinkability. The former means that one cannot identify the signer, while the latter says that no one can decide whether two signatures are generated by the same signer. The unconditional anonymity is a strong security notion that would be

a double edged sword: On one hand, it provides perfect privacy protection towards individual signing behavior. On the other hand, it could be abused for some illegal purpose such as wash trading. Therefore, some restrictions on anonymity should be taken into consideration. In fact, even ten years before the concept of ring signature, Chaum (Chaum and van Heyst, 1991) proposed the concept of group signature, which allows a group member to anonymously sign a message on behalf of the group, with the restriction that a designated group manager is able to identify the signer whenever it is necessary. One of the main differences between group signature and ring signature lies in that the ring structure is an ad hoc group that can be formed in an on-the-fly manner, while the group structure is formed under the control of the group manager. Furthermore, anyone who wants to join the group has to at first perform a registration process — either online or offline. In 2004, Liu et al. (Liu et al., 2004) proposed a linkable spontaneous anonymous group (LSAG) signature scheme, which is essentially a linkable ring signature considering the spontaneous group formation and no group manager (Sun et al., 2017). Recently, Liu et al.'s idea was adopted by Back (Back, 2015) in designing Ring-Coin with necessary improvements in efficiency. Along with another line, Fujisaki et al. (Fujisaki and Suzuki, 2007) in 2007 extended the concept of ring signature into the so called traceable ring signature by adding an issue related tag into the signature. In this case, anyone in the ring, pretending to be another person to sign the same message, would face the risk of revealing his/her identity immediately. This idea was adopted to prevent double-spending and now becomes the basis of CryptoNote (van Saberhagen, 2013) with a slight modification. However, either CryptoNote or Ring-Coin suffers from the possible attack based on the observation and analysis of the amounts sent in a given transaction (Noether, 2015). To hide amounts for any transaction, Maxwell (Maxwell, 2017) proposed the concept of the confidential transaction by using homomorphic commitment protocol.

Shortly afterward, Noether (Noether, 2015) offered a modification to the Monero protocol by coupling three techniques: Maxwell's confidential transaction, ring signature and multilayered linkable spontaneous, anonymous group signature (MLSAG). Noether's idea is now named as Ring Confidential Transactions for Monero (RingCT for short). In 2017, Sun et al. (Sun et al., 2017) proposed a non-trivial upgraded version towards RingCT, named as RingCT 2.0. Besides the rigorous formalization of the syntax of RingCT and formal security models, RingCT2.0 also applies some well-known cryptographic primitives, including Pedersen commitment, the accumulator with one-way domain and signature of knowledge, to obtain the significant storage and communication cost saving. More specifically, the signature size is reduced from $O(nm)$ to $O(m)$, where n and m are the numbers of groups and accounts in one group, respectively. In other words, the transaction size in RingCT 2.0 is independent of the number of groups in the ring, and this enables each block to process more transactions.

4.2 One-time (ring) signatures

Lamport in 1979 (Lamport, 1979) proposed the concept of one-time signature (OTS), where the signing key can be used securely but only once, and the signing key would be revealed if it is used twice or more. OTS is frequently used as a building block in constructions of encryptions and authenticated key agreements. By combining the ideas of OTS and ring signature, Saberhagen (van Saberhagen, 2013) proposed a new signature scheme where the private key can be used only once for signing on behalf of a group. Suppose that Bob's public key is (A, B) , and Alice wants to send a payment to Bob. Then, Alice can pick a random number $r \in \mathbb{F}_q$ and compute the transaction public key R and the destination key P as follows:

$$R = rG \text{ and } P = H_s(rA)G + B,$$

Where $H_s : \{0,1\}^* \rightarrow \mathbb{F}_q$ is a cryptographic hash function and G is the public base point of the elliptic curve $E(\mathbb{F}_q)$. Then, Bob can locate Alice's payment via checking every past transaction on the blockchain

with his private key pairs (a, b) to see if $P = H_s(aR)G + B$ holds. After locating Alice's payment, Bob can recover the corresponding one-time private key $x = H_s(aR) + b(6)$ and spend this output at any time by signing a transaction with x .

4.3 Borromean (ring) signatures

Another interesting primitive related to ring signature and blockchain is the so-called Borromean (ring) signature (BRS), proposed by Maxwell and Poelstra in 2015 (Maxwell and Poelstra, 2015). Poelstra (Poelstra, 2017) claimed that BRS is now used in Elements (Element, 2015), Liquid (Liquid) and Monero. Moreover, all of those projects are now being transited from the BRS-based range proofs to Bulletproofs (Bünz et al., 2017). In an abstract view, a ring signature is nothing than a signature that the signer knows one of secret keys for a given group, say $x_1 \vee x_2 \vee \dots \vee x_n$, while a Borromean ring signature extends this idea to the scenario where the signer knows one of secrets for each given group, say $(x_1 \vee x_2 \vee \dots) \wedge (y_1 \vee y_2 \vee \dots) \wedge \dots \wedge (z_1 \vee z_2 \vee \dots)$. Apparently, this idea gains the capability to express knowledge of any monotone boolean function of the signing keys (Maxwell and Poelstra, 2015). Although the primitive of attribute-based signature (ABS) (Majiet al., 2011) can also realize the formula by considering signing keys $x_1, x_2, \dots, y_1, y_2, \dots, z_1, z_2, \dots$ as attributes and modeling the signing capability as a tree-like access structure corresponding, there exists an essential difference between ABS and BRS. In particular, ABS focuses on who can generate a valid signature, while BRS focuses on how to aggregate multiple ring signatures anonymously. That is, the validations of all involved ring signatures in a BRS scheme are intertwined. If one of the ring signatures involved in the joint Borromean signature is invalid, then the entire signature is invalid, and you cannot tell which one is invalid (Poelstra, 2017). This is the very reason for the name Borromean ring signature. In topological, Borromean rings is a style of interlocking rings such that each ring goes through each other ring (Poelstra, 2017; Cromwell et al., 1998). The

construction of BRS scheme in reference (Maxwell and Poelstra, 2015) is based on an elegant combination of several efficient techniques, including Schnorr authentication (Schnorr, 1991), AOS ring signature (Abe et al., 2002), and the newly developed “halfchameleon hash” and “multiple chameleon hash”. Interested readers are suggested to refer (Maxwell and Poelstra, 2015) for more details.

4.4 Multi-signatures The primitive of multi

Signature allows a single signature to work as several ordinary signatures on the same message. One of the critical requirements of multi-signature is that the single signature has the same size as one regular signature. This primitive was introduced by (Itakura and Nakamura, 1983) in 1983 and has been studied over the past decades (Ohta and Okamoto, 1999; Okamoto, 1988; Boldyreva, 2002; Micali et al., 2001). Very recently, ZILLIQA team (Zilliqa) proposed the next generation high throughput blockchain platform by using an EC-Schnorr multi-signature protocol as one of its innovative ingredients. More specifically, the protocol in ZILLIQA consists of the following steps:

- The standard Schnorr signature scheme (Schnorr, 1991) is instantiated over the elliptic curve specified by secp256k1 (Certicom-Research, 2000).
- The above EC-Schnorr signature scheme for a single user is extended to an EC-Schnorr multi-signature scheme for multiple users based on the idea in reference (Micali et al., 2001).
- The above EC-Schnorr multi-signature is tweaked for PBFT (practical Byzantine fault tolerance) settings, where the message is required to be properly signed by at least $2n+1$ nodes in the committee.

V. HASH-BASED POST-QUANTUM DIGITAL SIGNATURES

5.1 One-Time Signatures

Hash-based signature schemes have been documented in the literature since 1979, thanks to the Lamport-OTS scheme. The logic behind Lamport's scheme is straightforward, the signer

generates pairs of random values per bit required to be signed and these pairs form the private key. The public key is formed by the hashes of those values. To sign a message, the signer reads the message bitwise and presents one value from each secret pair depending on the bit value. The verifier can then validate that the hashes of all the secret values are equal to the corresponding hash values in the public key.

Although Lamport-OTS hash computations are considered fast, key and signature sizes are relatively large. For instance, if SHA256 is used as the underlying hash function, the public key consists of 512 hashed outputs of 256 bits each (one hash-pair per bit), while the signature consists of 256 secret values (256 bits each). If we aggregate the above, the key and signature consist of 24.5 kB. Similarly, if SHA512 is applied, about 98 kB are required.

Further enhancements to the original algorithm, reduce the key size significantly. At present, the WOTS algorithm and its variants are considered some of the most efficient key and signature compression methods, while Bleichenbacher and Maurer's graph-based scheme attempts to achieve the best possible efficiency in terms of signature size and number of hash function evaluations per bit of the message.

As a note, one of the main differences between OTS approaches lies in the security assumptions of requiring (or not) collision resistant hash functions and the use of extra bitmasks. Currently, WOTS-T, proven to be secure in the QROM model, is considered one of the most promising candidates from the WOTS family, because only one extra seed value is required along with the public key to compute the required bitmasks, while its security is not affected by the birthday paradox and it also introduces keying of all hash function calls to prevent multi-target second pre-image attacks. The latter results in shorter public keys and hash-output sizes.

5.2 Few- and Many-Time Signatures

Although there exist multiple methods to turn a one-time into a multi-time signature scheme, a popular approach is to use Merkle authentication

trees by fixing beforehand the total number of signatures which will ever be produced. Using Merkle trees, the total number of signatures which can be issued is defined at key generation. The main benefit is its short signature output and fast verification, while the drawbacks are the relatively expensive key generation time and the fact that they are stateful. Figure 1 depicts a 4-time (at maximum) Merkle tree signature scheme.

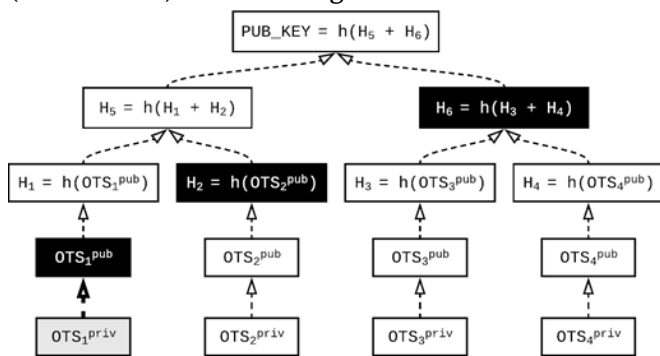


Fig. 1: Few-time Merkle tree signature scheme able to sign four messages in total. Dark nodes represent the authentication path required if we sign with OTS 1.

Moving to stateless few-time signatures requires extra complexity and larger signature outputs. HORS (and its extension HORST) is currently the one used in the majority of many-time stateless signature schemes, such as SPHINCS.

Many-time hash-based schemes can be constructed by combining the above {one and few} time constructions and they are grouped into two categories, stateful (e.g., XMSS, LMS) and stateless (e.g., SPHINCS, SPHINCS+, Gravity, Simpira, Haraka). Stateful schemes typically produce shorter signatures, but they need a mechanism to keep state (what paths/keys have already been used).

On the other hand, stateless schemes start with a moderately large Merkle tree or tree-layers at the top, but instead of using OTS signatures at the bottom, they use a few-time signature method. The latter allows them to pick indices randomly and thus no path-state tracking is required. The downside to stateless schemes is their signature size; for instance, in SPHINCS-256 each signature is 41 kB long.

It is highlighted that the distinction between few- and many- time hash-based signature schemes is not

always clear. In the literature, few-time usually refers to stateless schemes, such as BiBa, HORS and HORST, for which practical parameters allow multiple signing operations, but not enough signatures to be considered in many real-world applications. On the other hand, many-time schemes can be configured to allow highly interactive environments to reuse the same key- pair for many years. The authors of Gravity SPHINCS claim that 1 trillion (240) signatures is a reasonable upper bound, whilst SPHINCS-256 allows for a maximum of 1 quadrillion (250) signatures. In practice, one can parameterize a many-timescheme to support just a few or several signatures.

5.3 Speed and Security of Hash Functions

The underlying hash algorithm is of obvious importance to the overall security of the proposed scheme. Several factors influence the choice of algorithm, including speed, security level and availability; e.g., what hardware features can be leveraged to improve the runtime performance, and what implementations are available in existing, well-reviewed cryptography libraries.

The first thing to establish, however, is whether the algorithm is resilient to PQ attacks. The SHA-2 and SHA-3 algorithms support multiple digest sizes, namely 224, 256, 384 and 512 bits [36], [37]. We observe that by leveraging the improved search speed provided by Grover's algorithm, collision resistance can be reduced from a half to a third of the chosen digest size. Consequently, in the presence of large-scale quantum computers, 384-bit versions of SHA-2 and SHA-3 would provide 128 bits of security against collisions, whereas the 256-bit versions would only offer 85 bits.

Further, we observe that quantum pre-image attacks on 256-bit versions of SHA-2 and SHA-3 can be realised by 2153.8 and 2146.5 surface code cycles, respectively [38].

As a result of these two observations, SHA-256 is considered unsuitable for use in schemes basing their security on hash collision resistance, but it is still secure otherwise. It should also be mentioned that

PQ algorithms have fundamentally worse price-performance ratio than the classical vanOorschot-Wiener hash-collision circuits, even under optimistic assumptions regarding the speed of quantum computers [39].

From performance measurements presented in eBACS [40], we have evaluated the relative performance of SHA-2, SHA-3 and BLAKE2 on general-purpose CPUs. We have deliberately chosen an Intel, an AMD and an ARM processor to cover typical desktop and mobile units.

As can be seen from Table 1, the number of cycles per byte decreases with the size of the input. This is expected due to the small input sizes in this comparison and the block-wise operation mode of the hash functions. The rate of decrease naturally flattens out as the input grows beyond the blocksize.

It should also be noted that the different versions of SHA-3 generally performs worse than their SHA-2 counterparts. One of the reasons for this is the fact that SHA-1 and SHA-2 have better hardware support from modern processors, e.g., through instruction set extensions like the Intel® SHA Extensions.

Note that, despite not offering protection against length extension attacks, SHA-2 offers similar bit-level security to SHA-3. Typically, hash-based PQ schemes, including BPQS (Blockchain Post Quantum Signature), are not prone to such attacks and therefore, we consider SHA-2 to be a better alternative due to the performance benefits it offers.

If performance is of importance, one can also consider employing the less supported BLAKE2b [41] algorithm. We highlight, however, the lack of widespread library support compared to the aforementioned algorithms.

Table 1: Performance Metrics for SHA-2, SHA-3 and Blake

Input Size	Measurements of Hash Functions ^a								
	Cycles / Byte (relative to SHA2-256 on 8 byte input)								
	SHA-2			SHA-3			BLAKE2 ^b		
	Intel	AMD	ARM	Intel	AMD	ARM ^c	Intel	AMD	ARM
256-bit output									
8	1.00	0.19	2.99	3.48	2.89	6.78	0.47	0.38	2.30
64	0.24	0.04	0.54	0.46	0.38	0.85	0.05	0.04	0.28
576	0.13	0.02	0.20	0.25	0.21	0.40	0.05	0.04	0.15
512-bit output									
8	1.49	1.12	5.72	3.58	3.00	6.79	0.53	0.46	3.23
64	0.19	0.14	0.71	0.48	0.40	0.85	0.07	0.05	0.41
576	0.09	0.05	0.30	0.43	0.36	0.71	0.03	0.03	0.14

^aBased on numbers reported by ECRYPT II in eBACS [40].

Intel - amd64, genji122, supercop-20171020

AMD - amd64, genji262, supercop-20171020

ARM - armeabi, odroid, supercop-20160806

^bBLAKE2s with 32-bit words, 10 rounds, and 256-bit output; BLAKE2b with 64-bit words, 12 rounds, and 512-bit output.

^cNo data for SHA-3; numbers are for keccakc512/1024 with 256- and 512-bit output sizes, respectively. These are the Keccak team's final submissions for SHA-3-256 and SHA-3-512.

VI. BLOCKCHAINED POST-QUANTUM SIGNATURES TAILORED TO ONE-TIME KEYS

Most if not all few-time hash-based signature schemes make use of Merkle trees. The maximum number of messages a basic Merkle tree signature scheme can sign is 2^h , where h is the height of the tree. Also, all leaves (keys) should be computed during key generation in order to form the root. Due to the above, to construct a tree of height $h = 40$, key generation would be considered impractical, because we need to compute 240OTS keys and each OTS key internally requires many hash invocations (i.e., 512 hash invocations with LamportOTS or 67 for WOTS ($w = 16$) when using SHA256). The trick to keeping key generation time practical, while allowing for a large number of signatures is to use a multi-level tree.

BPQS is a simplified single-chain variant of the XMSS family protocols which are literally an extension of the basic Merkle tree signature scheme (see Figure 1). BPQS can theoretically sign many times, but its design focuses on short and fast one-time signatures with the extra option to re-sign if and when needed. The above requirement is what a typical blockchain or DLT requires, as the use of one-time keys is recommended to preserve anonymity. However, a lot of things can go wrong, e.g., a transaction might not go through or there might be a fork in the chain, in which case one

should be able to sign more than one time without compromising security or freezing assets.

An additional, surprising benefit of BPQS is that it is also an ideal candidate for the opposite requirement; signing multiple times with the same key. This interesting property is due to the underlying graph-structure of blockchain and DLT systems that effectively allow many-time signatures at a minimal cost compared to other hash-based PQ solutions. This works by referencing the block (or transaction) in which the same BPQS key has been used in the past. In short, only a small part of the new signature is required to be submitted and the rest of the path will be delegated to the previous transaction this key was used to sign. The latter enables us to complete the full path to the advertised root BPQS key. Actually, because previous transactions are verified on the ledger already, verifiers do not even need to validate the rest of the path, as it was inherently verified in the past. This characteristic makes BPQS very useful for notary-based DLTs, such as Corda and Fabric, as the notary nodes normally sign transactions with the same known key.

6.1 BPQS Scheme

BPQS requires an underlying OTS scheme. Although any OTS solution could in theory be applied, our scheme shares logic with the XMSS protocol family, hence the selection of the WOTS variant, use of L-Trees and generation of bitmasks (blinding masks) define the security assumptions and proofs, similarly to XMSS, its multi-level version XMSSMT and XMSS-T [27]. Also, according to, collision resistance is actually cheaper using quantum algorithms, and thus similarly to the Gravity SPHINCS scheme, bitmasks and L-Trees might be omitted.

One could state that BPQS is a subset of XMSS tailored to fast first-time signatures. The main difference is that XMSS overcomes the limitation to one message per key by using hash trees which reduce the authenticity of many OTS verification keys to one public XMSS root key. In contrast, BPQS

utilises a chain of small 2-leaf Merkle trees. Geometrically, XMSS grows in both width and height (see Figure 1), while BPQS grows on chain height only (see Figure 2). All in all, we stress that BPQS is a generic blockchained construction, where blocks are “tiny” Merkle trees, meaning that it can be parameterised according to the requirements of the application. In case blinding masks are applied, their deterministic generation should follow the same logic with the corresponding XMSS family scheme.

There are 2 basic building blocks of BPQS:

- BPQS-FEW, which strictly supports few-time signatures and is depicted in Figure 2(left),
- BPQS-EXT, which theoretically can be extended to support many-time signatures, see Figure 2(right).

In BPQS-FEW, all keys are precomputed during key generation, the penalty for each extra signature is just 1 extra hash output, but it cannot be extended to practically support “unlimited” signatures.

On the other hand, BPQS-EXT initially requires only two OTS keys and in contrast to BPQS-FEW, the left leaf in each 2-leaf Merkle tree is an OTS fallback key that can be used to sign the next signature block when required. Unfortunately, the extensibility property comes with the cost of requiring one extra WOTS key per new signature.

The full BPQS scheme combines both BPQS-FEW and BPQS-EXT in a way where the last leaf in the chain of BPQS-FEW is a BPQS-EXT fallback key. This trick allows us to convert the few-time variant to a many-time one. Actually, BPQS-EXT can be considered a special case of BPQS, in which there is no initial BPQS-FEW chain.

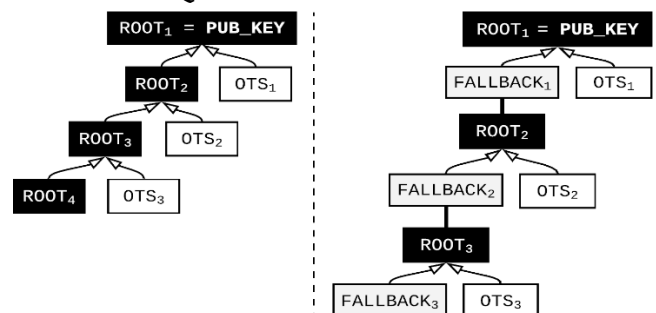


Fig. 2: BPQS-FEW (left), a few-time signature scheme. BPQS-EXT (right), a linearly extensible many-time signature scheme.

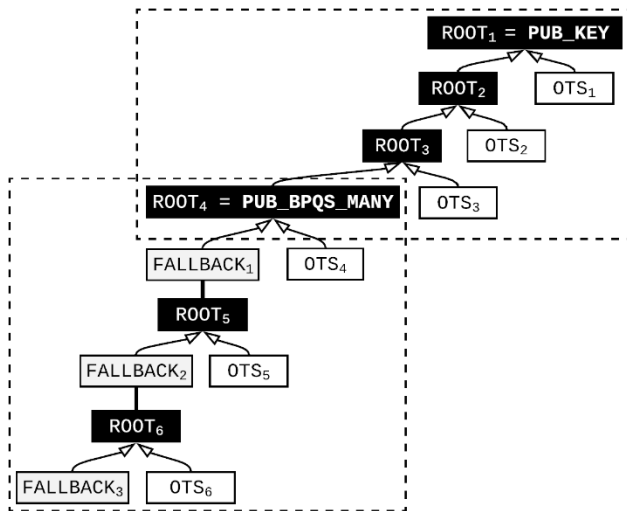


Fig. 3: Full BPQS protocol, with a height-3 BPQS-FEW top-level and a BPQS-EXT fallback key to allow for extensibility.

Parameters for BPQS include:

- the WOTS variant used (e.g., WOTS-T[27]),
- the Winternitz parameter (e.g., $w = 16$), which defines the base at which the initial hash is interpreted. Similarly to XMSS [5], w defines the actual size of each WOTS chain, which in turn affects signature size. Note that there is no consistency on the interpretation of the Winternitz parameter in the literature. For instance, in LMS [45] it is defined as 2^w and thus $w_{BPQS} = 16 = 2^4$ would be equivalent to $w_{LMS} = 4$,
- the underlying hash function (i.e., SHA384),
- the number of precomputed OTS keys, meaning the initial height (e.g., $h = 4$).

6.2 BPQS Mixed

The extensibility property of BPQS enables various custom constructions. BPQS can be used as a building block to convert any hash-based signature scheme into a {first or few} time optimised one. For instance, in Figure 4, BPQS-FEW is used for the first (shorter) signatures and then it fallbacks to another PQ scheme. Although in the depicted approach the key-pair of the fallback (other) PQ scheme should be a-priori known and precomputed, one could use the BPQS-EXT in a similar fashion, so that this is not necessarily a requirement and the “other” PQ key will be generated only after the few-time signatures

are exhausted. Moreover, if the “other” PQ scheme is stateless, such as SPHINCS, the final protocol is literally a “startstatefulhengo stateless” scheme.

It should be emphasized that the “other” PQ scheme might be another BPQS scheme, so one could eventually create a chain of different BPQS schemes. The latter would result in shorter signatures versus just extending it with BPQS-EXT each time.

With regards to the “Other PQ Key Params” shown in Figure 4, it is important that some schemes are required to publish bitmasks (or a seed in XMSS-T [27]) as part of the initial advertised public key. Otherwise, it would allow an adversary to select the seed/bitmask in a forgery. However, if BPQS uses a hash function with a bigger output (e.g., SHA384 or SHA512) this might not be necessary, because the provided security-level against potential quantum collision

attacks would still be enough to prevent such attacks.

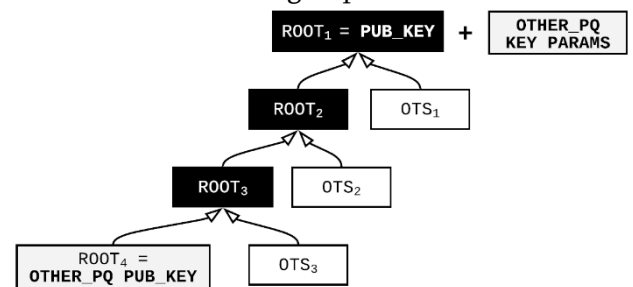


Fig. 4: A versatile BPQS protocol (BPQS-VERS1), with a BPQS-FEW top-level of height 3, in which the last root is the public key of another PQ scheme, such as XMSSMT [44] or SPHINCS + [32].

6.3 Combined PQ Schemes

As already mentioned, BPQS can fallback to another PQ scheme whenever required. By applying a similar logic,

Figure 5 shows various custom models for combining multiple PQ schemes into one. The approach is very simple, but allows for very useful constructions, such as a “Stateful and Stateless” scheme in Figures 5 A and B, or a “Stateful with Stateless Fallback” scheme in Figure 5 C. The latter provides a solution to clustered environments in which multiple nodes require consensus over signature states, but a fallback

mechanism is a prerequisite for the system to stay functional if consensus fails for any reason.

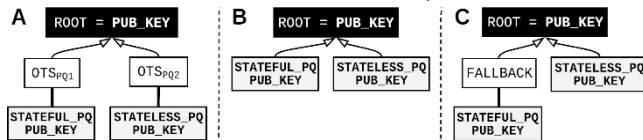


Fig. 5: Various recommended designs using a parallel BPQS logic to combine multiple schemes into one concrete PQ solution. Note that if the underlying schemes require extra parameters, such as bitmasks, these should be published along with the root public key, similarly to Figure 4.

The three depicted approaches offer different flexibility when it comes to:

1. Choosing a balance between key generation time and size of signature,
2. Deciding whether to allow for picking of the underlying algorithms at a later time.

For instance, option B requires both PQ keys to be generated to form the to-be-advertised combined public key, whilst option A is practically a BPQS-EXT that will be used to sign the “upcoming” PQ schemes. Along the same lines, option C is a combination of A and B, but the left PQ scheme is not required to be a-priori selected and computed. Note that one could even combine two different stateful or stateless schemes together, e.g., if needed for compatibility purposes, such as when using the same key in two different blockchains, one supporting the original SPHINCS-256 and the other supporting a variation of it (or its standardised version when this becomes available).

VII. CONCLUSION

In this work, we introduced BPQS and its extensions to support {one and few}-time optimised post-quantum signatures. We have also presented the security challenges that blockchains and DLTs will soon face and why pure OTS schemes are not recommended as a quantum-resistant replacement. As shown, BPQS compares favourably even against conventional non-quantum schemes such as RSA,

ECDSA and EdDSA, while it provides more reliable quantum-security estimates because of its rooting in a secure cryptographic hash function.

Among others, the main features of the BPQS protocol are:

- shorter signatures, and faster key generation, signing and verification times than the XMSS[5] and SPHINCS [23] family PQ protocols when signing for one or few times, which is usually preferred in blockchain systems to preserve anonymity,
- it is computationally comparable to non-quantum schemes. One can take advantage of the easy-to-apply multiple hash-chain WOTS parallelisation and caching to provide almost instant signing and fast verification,
- its extensibility property allows for many-timesignatures, while it can also easily be customised, so it can fallback to another many-timescheme if and when required,
- when used in blockchain and DLT applications, it can take advantage of the underlying chain/graph structure by referencing a previous transaction, in which the same key is reused. This could effectively mean that each new BPQS signature simply requires the effort of an OTS scheme, because the rest of the signature path to the root is in the ledger already and can be omitted,
- it could be used as a building block to implement novel PQ schemes such as a simultaneously “Stateful and Stateless” scheme, which might benefit clustered environments, where nodes can fallback to stateless schemes when consensus is lost. Additionally, such schemes can be used for forward and backward compatibility purposes or when requiring to reuse a key between two independent and incompatible blockchains.

The main drawback of the original BPQS protocol is that the size of its signature output increases linearly with the number of signatures. However, one can mitigate this by using a combined PQ approach or by utilising existing graph structures in blockchain applications. All in all, the customisation, caching and extensibility properties of BPQS make it an ideal

candidate for blockchains and it could serve as a bridging protocol between stateless, stateful and other PQ schemes.

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